



Chapter 3, sections 3.1-3.3.4:
Feature Structures

Problems with Context-free Grammar

- Potentially arbitrary rules
- Gets clunky quickly with cross-cutting properties
- Not quite powerful enough for natural languages

Solution: Replace atomic node labels with feature structures.

Cross-cutting Grammatical Properties

	3rd singular subject	plural subject
direct object NP	<i>denies</i>	<i>deny</i>
no direct object NP	<i>disappears</i>	<i>disappear</i>

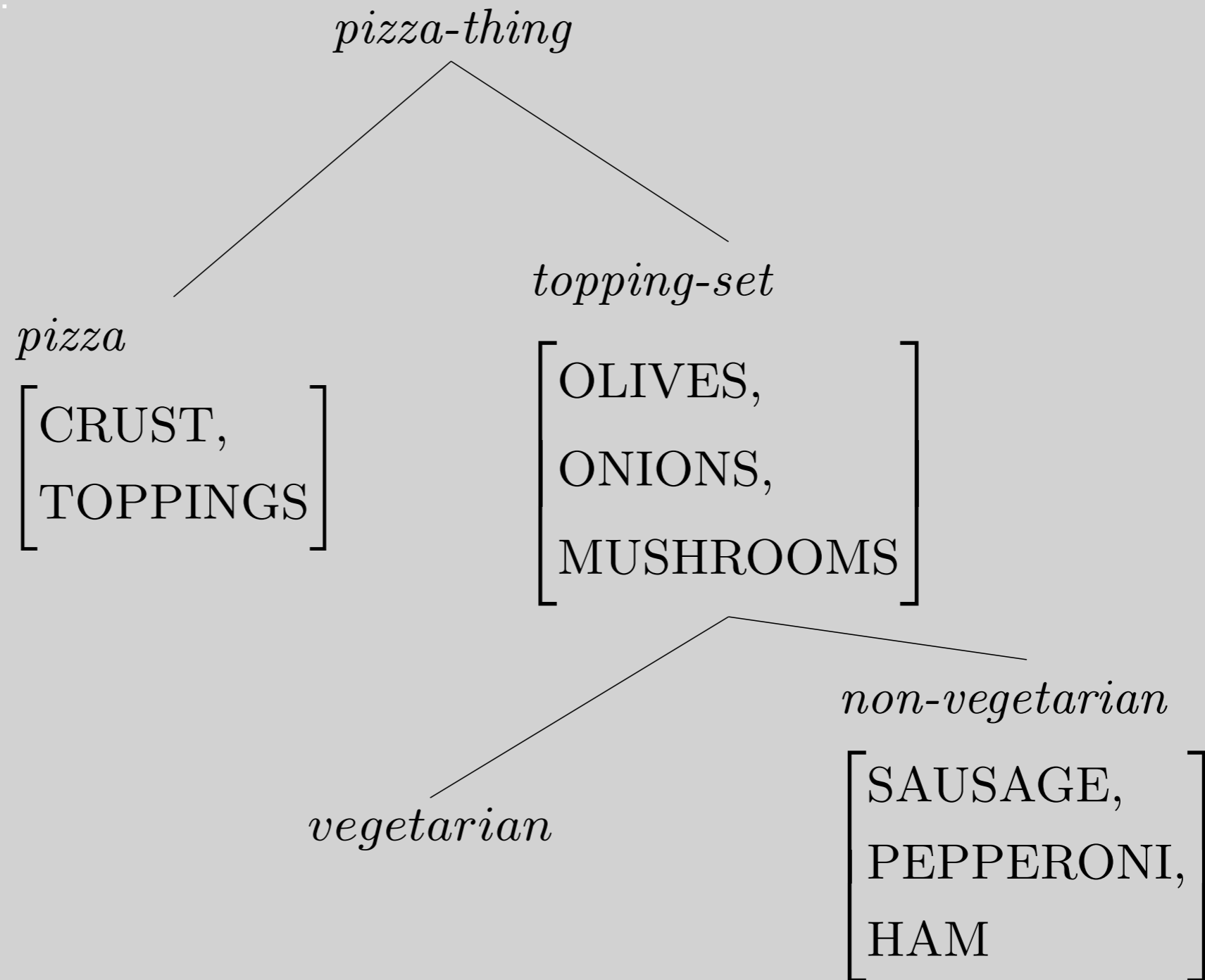
Things Involved in Modeling Language

- Real world entities
- Models
- Descriptions of the models

Feature Structure Descriptions

FEATURE ₁	VALUE ₁
FEATURE ₂	VALUE ₂
...	
FEATURE _n	VALUE _n

A Pizza Type Hierarchy



TYPE	FEATURES/VALUES	IST
<i>pizza-thing</i>		
<i>pizza</i>	$\left[\begin{array}{ll} \text{CRUST} & \{ \text{thick, thin, stuffed} \} \\ \text{TOPPINGS} & \text{topping-set} \end{array} \right]$	<i>pizza-thing</i>
<i>topping-set</i>	$\left[\begin{array}{ll} \text{OLIVES} & \{ +, - \} \\ \text{ONIONS} & \{ +, - \} \\ \text{MUSHROOMS} & \{ +, - \} \end{array} \right]$	<i>pizza-thing</i>
<i>vegetarian</i>		<i>topping-set</i>
<i>non-vegetarian</i>	$\left[\begin{array}{ll} \text{SAUSAGE} & \{ +, - \} \\ \text{PEPPERONI} & \{ +, - \} \\ \text{BBQ CHICKEN} & \{ +, - \} \end{array} \right]$	<i>topping-set</i>

Type Hierarchies

- A type hierarchy....
- ... states what kinds of objects we claim exist (the types)
- ... organizes the objects hierarchically into classes with shared properties (the type hierarchy)
- ... states what general properties each kind of object has (the feature and feature value declarations).

Pizza Descriptions and Pizza Models

$$\left[\begin{array}{l} \textit{pizza} \\ \text{CRUST} \quad \text{thick} \\ \text{TOPPINGS} \quad \left[\begin{array}{l} \textit{vegetarian} \\ \text{OLIVES} \quad + \\ \text{ONIONS} \quad + \end{array} \right] \end{array} \right]$$

How many pizza models (by definition, fully resolved) satisfy this description?

Answer: 2

$$\left[\begin{array}{l} \textit{pizza} \\ \text{CRUST} \quad \text{thick} \\ \text{TOPPINGS} \quad \left[\begin{array}{l} \textit{vegetarian} \\ \text{OLIVES} \quad + \\ \text{ONIONS} \quad + \end{array} \right] \end{array} \right]$$

{<CRUST , thick> , <TOPPINGS , { <OLIVES , + > ,
<ONIONS, +> , <MUSHROOMS, ->}>}

{<CRUST , thick> , <TOPPINGS , { <OLIVES , + > ,
<ONIONS, +> , <MUSHROOMS, +>}>}

Pizza Descriptions and Pizza Models

$$\left[\begin{array}{l} \textit{pizza} \\ \text{CRUST} \quad \text{thick} \\ \text{TOPPINGS} \quad \left[\begin{array}{l} \textit{vegetarian} \\ \text{OLIVES} \quad + \\ \text{ONIONS} \quad + \end{array} \right] \end{array} \right]$$

How many pizzas-in-the-world do the pizza models correspond to?

Answer: A large, constantly-changing number.

Pizza Descriptions and Pizza Models

<i>pizza</i>							
CRUST	thick						
TOPPINGS	<table><tr><td><i>vegetarian</i></td><td></td></tr><tr><td>OLIVES</td><td>+</td></tr><tr><td>ONIONS</td><td>+</td></tr></table>	<i>vegetarian</i>		OLIVES	+	ONIONS	+
<i>vegetarian</i>							
OLIVES	+						
ONIONS	+						

‘type’/‘token’ distinction -- applies to sentences as well

Combining Constraints

$$\left[\begin{array}{l} \textit{pizza} \\ \text{CRUST} \\ \text{TOPPINGS} \end{array} \right] \begin{array}{l} \text{thick} \\ \left[\begin{array}{l} \text{OLIVES} \\ \text{HAM} \end{array} \right] \begin{array}{l} + \\ - \end{array} \end{array} \quad \& \quad \left[\begin{array}{l} \textit{pizza} \\ \text{TOPPINGS} \end{array} \right] \left[\begin{array}{l} \text{OLIVES} \\ \text{ONIONS} \end{array} \right] \begin{array}{l} + \\ + \end{array} \right]$$

Combining Constraints

<i>pizza</i>	
CRUST	thick
	[OLIVES +]
TOPPINGS	[ONIONS +]
	[HAM -]

Combining Constraints

$$\left[\begin{array}{l} \textit{pizza} \\ \text{CRUST} \\ \text{TOPPINGS} \end{array} \begin{array}{l} \text{thick} \\ \left[\begin{array}{l} \text{OLIVES} \\ \text{HAM} \end{array} \right] \begin{array}{l} + \\ - \end{array} \end{array} \right] \& \left[\begin{array}{l} \textit{pizza} \\ \text{CRUST} \\ \text{TOPPINGS} \end{array} \begin{array}{l} \text{thin} \\ \left[\begin{array}{l} \text{OLIVES} \\ \text{ONIONS} \end{array} \right] \begin{array}{l} + \\ + \end{array} \end{array} \right] \\ = \square$$

Combining Constraints

$$\left[\begin{array}{l} \textit{pizza} \\ \text{CRUST} \\ \text{TOPPINGS} \end{array} \right] \left[\begin{array}{l} \text{thick} \\ \left[\begin{array}{l} \text{OLIVES} \\ \text{HAM} \end{array} \right] \end{array} \right] + \left[\begin{array}{l} \text{thick} \\ \left[\begin{array}{l} \text{OLIVES} \\ \text{HAM} \end{array} \right] \end{array} \right] \& \left[\begin{array}{l} \textit{pizza} \\ \text{CRUST} \\ \text{TOPPINGS} \end{array} \right] \left[\begin{array}{l} \text{thick} \\ \textit{vegetarian} \end{array} \right]$$

=

Combining Constraints

$$\left[\begin{array}{l} \textit{pizza} \\ \text{CRUST} \\ \text{TOPPINGS} \end{array} \right] \begin{array}{l} \text{thick} \\ \left[\begin{array}{l} \text{OLIVES} \\ \text{HAM} \end{array} \right] \end{array} + \left[\begin{array}{l} \text{thick} \\ \left[\begin{array}{l} \text{OLIVES} \\ \text{HAM} \end{array} \right] \end{array} \right] \& \left[\begin{array}{l} \textit{pizza} \\ \text{CRUST} \\ \text{TOPPINGS} \end{array} \right] \begin{array}{l} \text{thick} \\ \textit{vegetarian} \end{array}$$

= \square

A New Theory of Pizzas

pizza :

CRUST	{ thick , thin , stuffed }
ONE-HALF	<i>topping-set</i>
OTHER-HALF	<i>topping-set</i>

Combining Constraints

$$\begin{array}{l} \left[\begin{array}{l} \textit{pizza} \\ \text{ONE-HALF} \end{array} \right] \left[\begin{array}{l} \text{ONIONS} \quad + \\ \text{OLIVES} \quad - \end{array} \right] \quad \& \quad \left[\begin{array}{l} \textit{pizza} \\ \text{OTHER-HALF} \end{array} \right] \left[\begin{array}{l} \text{ONIONS} \quad - \\ \text{OLIVES} \quad + \end{array} \right] \\ \\ = \\ \left[\begin{array}{l} \textit{pizza} \\ \text{ONE-HALF} \\ \text{OTHER-HALF} \end{array} \right] \left[\begin{array}{l} \text{ONIONS} \quad + \\ \text{OLIVES} \quad - \\ \text{ONIONS} \quad - \\ \text{OLIVES} \quad + \end{array} \right] \end{array}$$

Identity Constraints (tags)

<i>pizza</i>					
CRUST	thin				
ONE-HALF	<table><tr><td>OLIVES</td><td>1</td></tr><tr><td>ONIONS</td><td>2</td></tr></table>	OLIVES	1	ONIONS	2
OLIVES	1				
ONIONS	2				
OTHER-HALF	<table><tr><td>OLIVES</td><td>1</td></tr><tr><td>ONIONS</td><td>2</td></tr></table>	OLIVES	1	ONIONS	2
OLIVES	1				
ONIONS	2				

Combining Constraints

$$\left[\begin{array}{l} \textit{pizza} \\ \text{ONE-HALF} \\ \text{OTHER-HALF} \end{array} \begin{array}{l} \boxed{1} \\ \boxed{1} \end{array} \left[\begin{array}{l} \text{ONIONS} \\ \text{OLIVES} \end{array} \begin{array}{l} + \\ - \end{array} \right] \& \left[\begin{array}{l} \textit{pizza} \\ \text{OTHER-HALF} \end{array} \left[\begin{array}{l} \text{MUSHROOMS} \\ \text{OLIVES} \end{array} \begin{array}{l} - \\ - \end{array} \right] \right]$$

=

$$\left[\begin{array}{l} \textit{pizza} \\ \text{ONE-HALF} \\ \text{OTHER-HALF} \end{array} \begin{array}{l} \\ \boxed{1} \\ \boxed{1} \end{array} \left[\begin{array}{l} \text{ONIONS} \\ \text{OLIVES} \\ \text{MUSHROOMS} \end{array} \begin{array}{l} + \\ - \\ - \end{array} \right] \right]$$

Note

$$\left[\begin{array}{l} \textit{pizza} \\ \\ \text{ONE-HALF} \\ \\ \text{OTHER-HALF} \end{array} \right] \begin{array}{l} \\ \\ \boxed{1} \\ \\ \boxed{1} \end{array} \left[\begin{array}{l} \text{ONIONS} \\ \text{OLIVES} \\ \text{MUSHROOMS} \end{array} \right] \begin{array}{l} + \\ - \\ - \end{array}$$

=

$$\left[\begin{array}{l} \textit{pizza} \\ \text{ONE-HALF} \\ \\ \text{OTHER-HALF} \end{array} \right] \begin{array}{l} \boxed{1} \\ \\ \boxed{1} \end{array} \left[\begin{array}{l} \text{ONIONS} \\ \text{OLIVES} \\ \text{MUSHROOMS} \end{array} \right] \begin{array}{l} + \\ - \\ - \end{array}$$

Combining Constraints

$$\left[\begin{array}{l} \textit{pizza} \\ \text{ONE-HALF} \\ \text{OTHER-HALF} \end{array} \right] \left[\begin{array}{l} \boxed{1} \left[\begin{array}{l} \text{ONIONS} \\ \text{OLIVES} \end{array} \right] \\ \boxed{1} \textit{vegetarian} \end{array} \right] \& \left[\begin{array}{l} \textit{pizza} \\ \text{ONE-HALF} \\ \left[\begin{array}{l} \text{SAUSAGE} \\ \text{HAM} \end{array} \right] \end{array} \right]$$

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Linguistic Application of Feature Structures: Making the Mnemonic Meaningful

What do these CFG categories have in common?

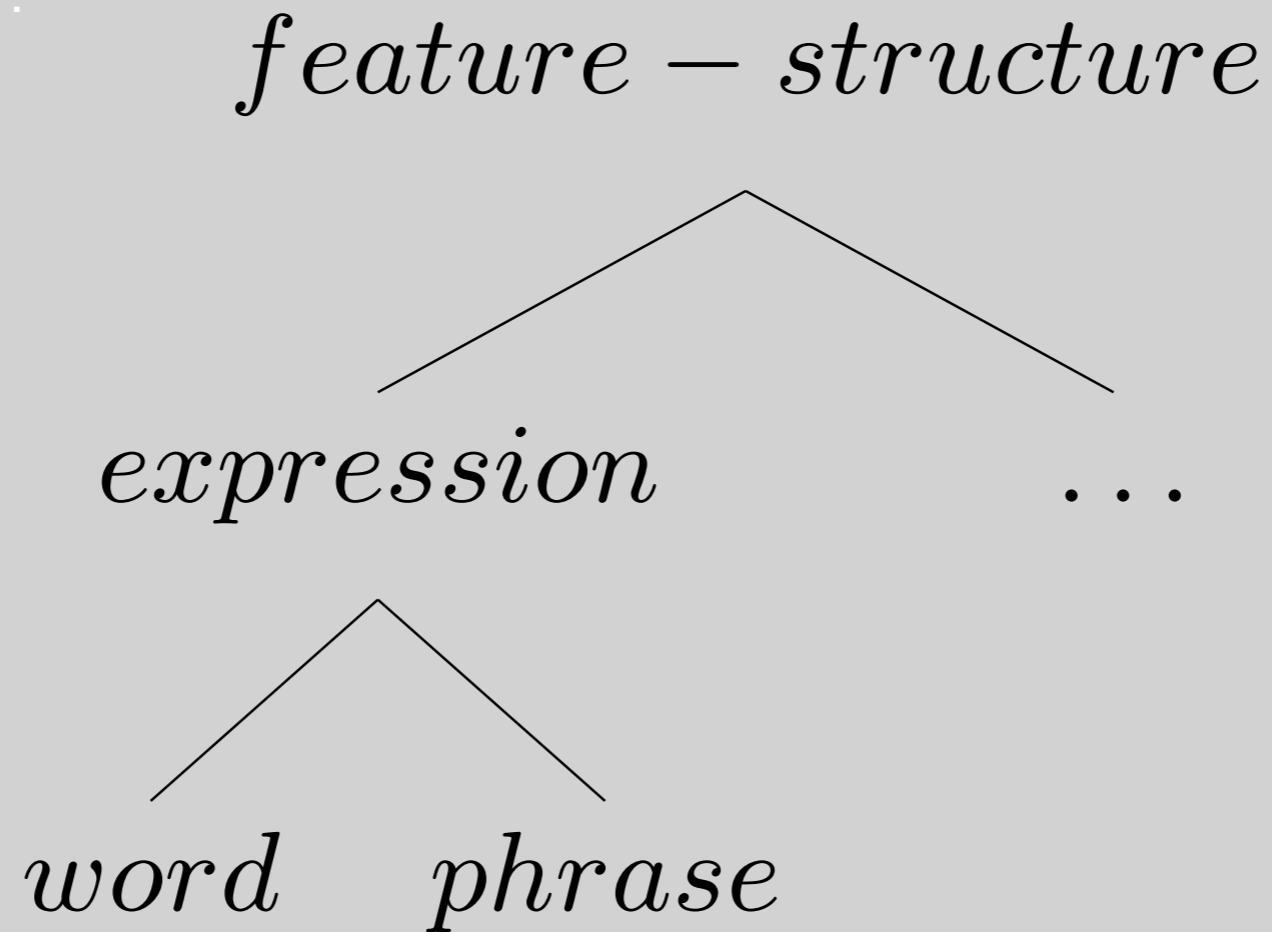
NP & VP: are both phrases

N & V: are both words

NP & N: are both ‘nouny’

VP & V: are both ‘verby’

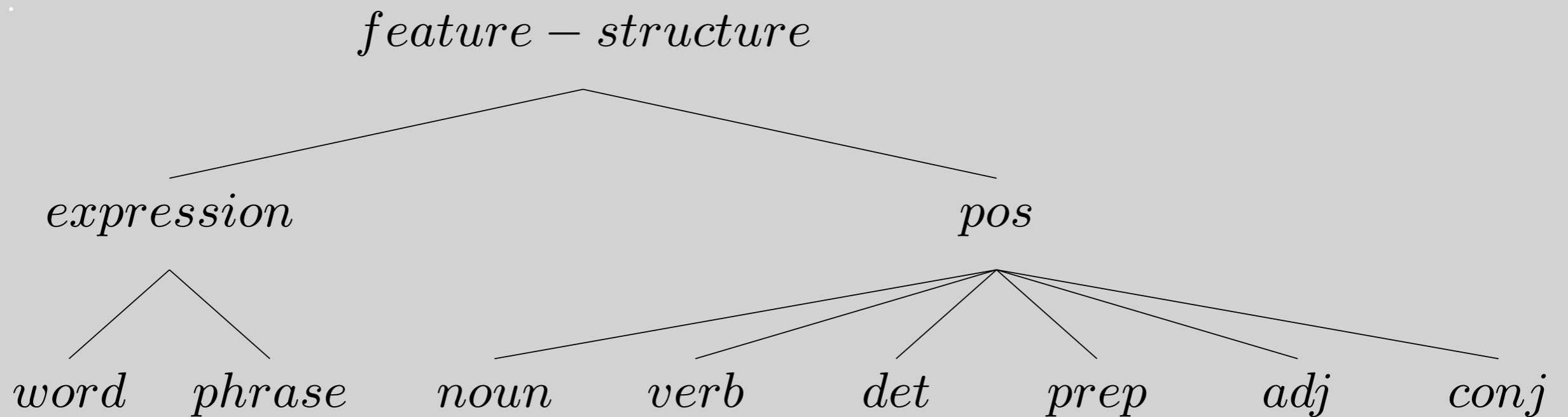
The Beginnings of Our Type Hierarchy



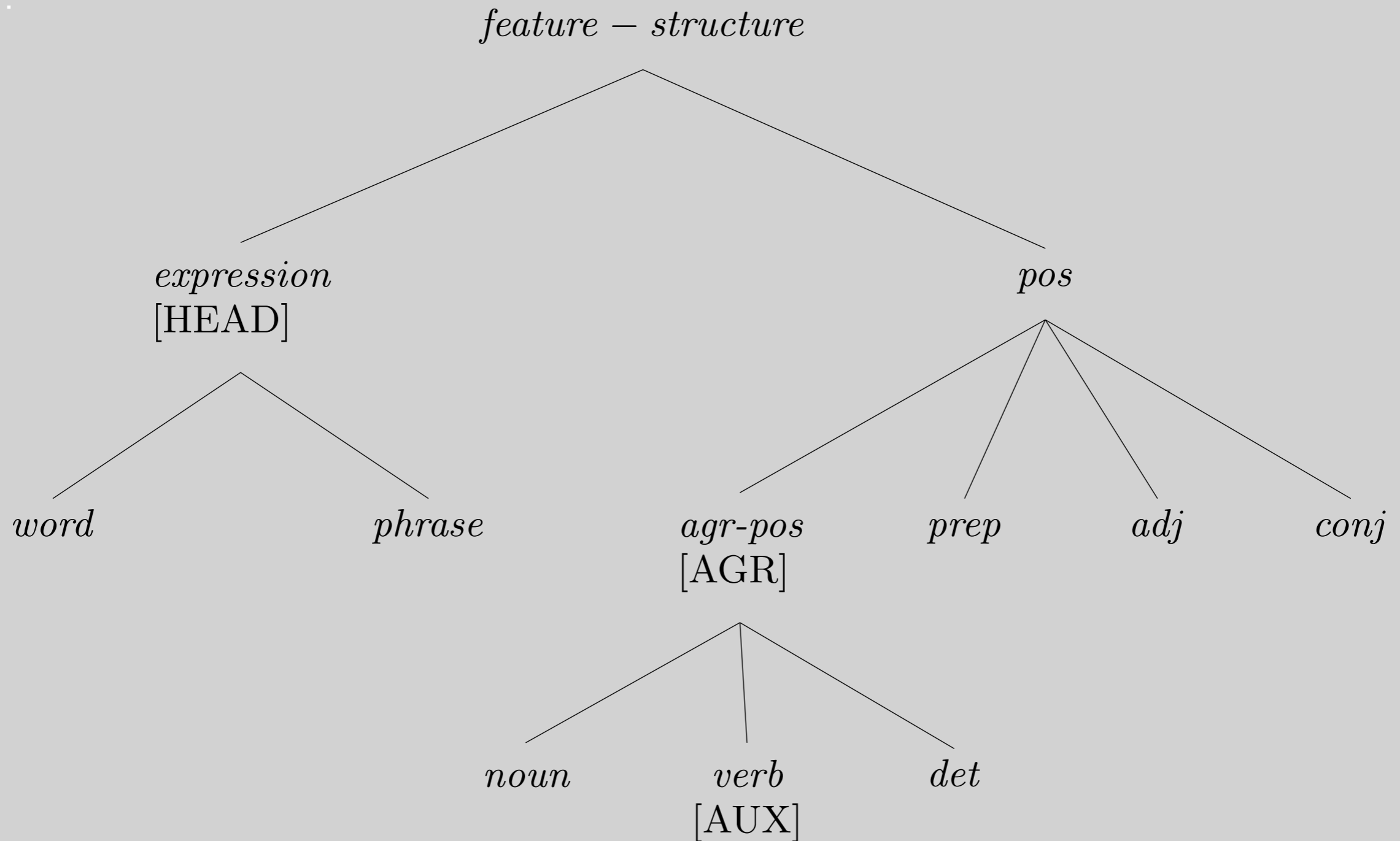
A Feature for Part of Speech

$$\text{NP} = \left[\begin{array}{l} \textit{phrase} \\ \text{HEAD} \quad \textit{noun} \end{array} \right]$$
$$\left\langle \text{bird} , \left[\begin{array}{l} \textit{word} \\ \text{HEAD} \quad \textit{noun} \end{array} \right] \right\rangle$$

Type Hierarchy for Parts of Speech I



Type Hierarchy for Parts of Speech II



A Feature for Valence

$$IV = \begin{bmatrix} \textit{word} \\ \text{HEAD} & \textit{verb} \\ \text{VAL} & [\text{COMPS} \quad \textit{itr}] \end{bmatrix}$$

$$TV = \begin{bmatrix} \textit{word} \\ \text{HEAD} & \textit{verb} \\ \text{VAL} & [\text{COMPS} \quad \textit{str}] \end{bmatrix}$$

$$DTV = \begin{bmatrix} \textit{word} \\ \text{HEAD} & \textit{verb} \\ \text{VAL} & [\text{COMPS} \quad \textit{dtr}] \end{bmatrix}$$

Underspecification

$$V = \begin{bmatrix} \textit{word} \\ \text{HEAD} \quad \textit{verb} \end{bmatrix}$$

$$VP = \begin{bmatrix} \textit{phrase} \\ \text{HEAD} \quad \textit{verb} \end{bmatrix}$$

$$[\text{HEAD} \quad \textit{verb}]$$

Another Valence Feature

$$\text{NP} = \begin{bmatrix} \textit{phrase} \\ \text{HEAD} & \textit{noun} \\ \text{VAL} & \begin{bmatrix} \text{COMPS} & \textit{itr} \\ \text{SPR} & + \end{bmatrix} \end{bmatrix}$$

$$\text{NOM} = \begin{bmatrix} \textit{phrase} \\ \text{HEAD} & \textit{noun} \\ \text{VAL} & \begin{bmatrix} \text{COMPS} & \textit{itr} \\ \text{SPR} & - \end{bmatrix} \end{bmatrix}$$

SPR and Verbs

$$S = \left[\begin{array}{l} \textit{phrase} \\ \text{HEAD} \quad \textit{verb} \\ \text{VAL} \quad \left[\begin{array}{l} \text{COMPS} \quad \textit{itr} \\ \text{SPR} \quad + \end{array} \right] \end{array} \right]$$

$$VP = \left[\begin{array}{l} \textit{phrase} \\ \text{HEAD} \quad \textit{verb} \\ \text{VAL} \quad \left[\begin{array}{l} \text{COMPS} \quad \textit{itr} \\ \text{SPR} \quad - \end{array} \right] \end{array} \right]$$

S and NP

$$\left[\text{VAL} \left[\begin{array}{l} \text{COMPS} \quad \text{itr} \\ \text{SPR} \quad \quad + \end{array} \right] \right]$$

- *We created a monster*
- *our creation of a monster*

Type Hierarchy for Parts of Speech II

feature – structure

